

**Optical studies of charge dynamics in optimally doped  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$** 

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Systematic temperature-dependent optical studies of optimally doped  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$  (OP Bi2212) single crystals have been carried out. An electron-boson spectral function peaked at 43 meV is derived in the normal state at 100 K, indicating that the most significant spectral feature in OP Bi2212 is a resonance at 43 meV. The optical data below  $T_c$  show that this boson is directly involved in the pair formation in OP Bi2212. Origins of the 43 meV mode are discussed.

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For Bardeen-Cooper-Schrieffer (BCS) superconductors, the spectral function  $\alpha^2F(\omega)$  contains all the relevant information concerning superconductivity.<sup>1</sup> Experimentally,  $\alpha^2F(\omega)$  is commonly obtained from tunneling  $I$ - $V$  curves using the well-developed Eliashberg theory.<sup>2</sup> In principle the optical conductivity can also be used to determine  $\alpha^2F(\omega)$  for BCS superconductors.<sup>3-5</sup> Recently, it has been recognized that the same kind of analysis of the optical data can give rise to a spectral function  $W(\omega)$  for  $d$ -wave high- $T_c$  superconductors.<sup>6</sup> This has led to the conclusion that electron coupling to the spin fluctuations<sup>7</sup> may be the analog to the common electron-phonon interaction in BCS superconductors. The issue of electron-boson coupling in high- $T_c$  cuprates has attracted much attention recently particularly due to the suggestion of strong electron-phonon interactions in these systems.<sup>8</sup> We will take a more empirical approach to discuss the experimental evidence of electron-boson coupling using optical data for different high- $T_c$  superconductors.<sup>9</sup>

In this paper, we report a detailed analysis of the electron-boson interaction in optimally doped  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$  (OP Bi2212) using new optical data. A bosonic spectral function peaked at 43 meV is identified in the normal state at 100 K. The optical data below  $T_c$  suggest that this 43 meV boson is directly involved in pair formation in OP Bi2212. The possibility of a resonant interaction of the spin resonance at 43 meV with a 44 meV phonon below  $T_c$  is discussed.

The  $ab$ -plane optical reflectance of OP Bi2212 has been measured previously.<sup>10</sup> However our systematic optical studies, with  $E\parallel a$ ,  $b$ , and  $c$  axes, have revealed many new features. Large OP Bi2212 single crystals are grown using the floating-zone method for this work and the crystals are mounted on an optically black cone. The polarized reflectance from 6 K to 295 K is measured in a near-normal incidence arrangement from  $\approx 30$  to over  $20\,000\text{ cm}^{-1}$  on a Bruker IFS 66v/S. The absolute reflectance is determined by evaporating a gold film *in situ* in vacuum ( $\approx 1 \times 10^{-8}$  Torr) over the sample.<sup>11</sup> The optical properties are determined from a Kramers-Kronig analysis.

In Fig. 1, raw optical data are shown for an OP Bi2212 single crystal. With  $E\parallel a$  axis, two in-plane optic phonons at 473 and 613  $\text{cm}^{-1}$  have been observed in reflectivity measurements. The temperature-dependent reflectance is given in Fig. 1(a) from about 100 to  $2000\text{ cm}^{-1}$ , and the optical con-

ductivity  $\sigma_1(\omega)$  is presented in Fig. 1(b). The optical conductivity is quite isotropic in the  $ab$  plane for OP Bi2212; however, large phonon anisotropy is observed as shown in the inset of Fig. 1 at 295 K. Particularly, the 473  $\text{cm}^{-1}$  phonon is absent for  $E\parallel b$  axis while a new mode appears at 350  $\text{cm}^{-1}$  or 44 meV. In addition, ten  $c$ -axis infrared-active phonons are observed instead of the  $6A_{2u}$  phonons that are predicted by the  $D_{4h}$  space group for OP Bi2212.<sup>12</sup> A more detailed theoretical analysis is needed to account for these new experimental findings.

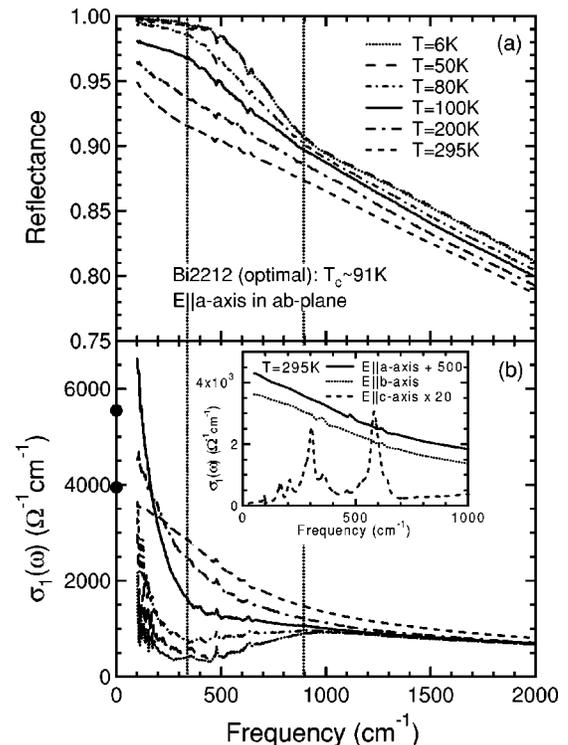


FIG. 1. The temperature-dependent  $ab$ -plane optical data of an OP Bi2212 single crystal with the  $E\parallel a$  from 100 to  $2000\text{ cm}^{-1}$ . (a) The temperature-dependent reflectance and (b) the temperature-dependent  $\sigma_1(\omega)$ . [The dots at zero frequency correspond to dc resistivity measurements at 200 K and 295 K, respectively. The two vertical lines at  $339\text{ cm}^{-1}$  (42 meV) and at  $893\text{ cm}^{-1}$  (111 meV) serve as guides to the eye.] Inset:  $\sigma_1(\omega)$  at 295 K for different polarizations ( $E\parallel a$  curve is offset for clarity).

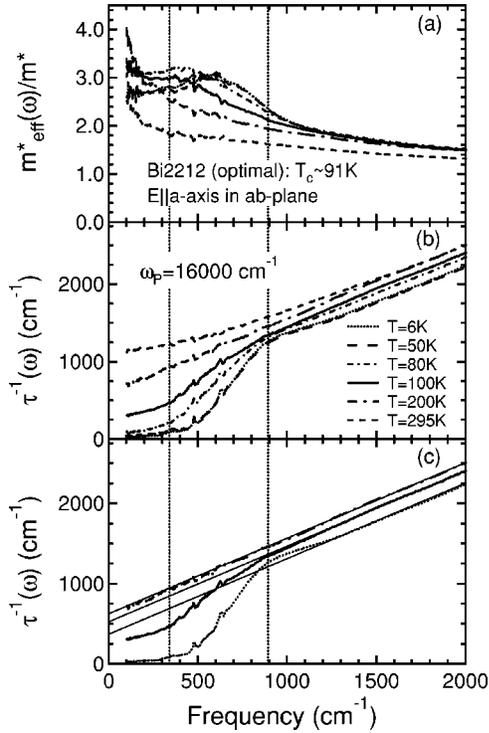


FIG. 2. The analysis of the *ab*-plane optical data of an OP Bi2212 single crystal with the  $E||a$  from 100 to 2000  $\text{cm}^{-1}$ . (a) The temperature-dependent mass ratio, (b) the temperature-dependent  $\tau^{-1}(\omega)$ , and (c)  $\tau^{-1}(\omega)$  is analyzed at 6, 100, and 200 K.

The conductivity data is analyzed in the extended-Drude formalism<sup>13</sup> with a frequency-dependent scattering rate  $\tau^{-1}(\omega)$  and a mass ratio that are defined as

$$\tau^{-1}(\omega) = \frac{\omega_p^2}{4\pi} \text{Re} \left[ \frac{1}{\tilde{\sigma}} \right], \quad \frac{m_{eff}^*}{m^*} = \frac{\omega_p^2}{4\pi\omega} \text{Im} \left[ \frac{1}{\tilde{\sigma}} \right], \quad (1)$$

where  $\omega_p$  is the classical plasma frequency. The value of  $\omega_p = 16000 \text{ cm}^{-1}$  is derived from the optical conductivity sum rule at 295 K. The results of such an analysis are given in Fig. 2. The temperature-dependent mass ratio is shown in Fig. 2(a) and the scattering rate  $\tau^{-1}(\omega)$  in Fig. 2(b). The frequency-dependent scattering  $\tau^{-1}(\omega)$  contains all the relevant information concerning the electron-boson interaction.<sup>3-5</sup> Because of the unprecedented signal-to-noise ratio ( $\approx 1000$ ) of these optical data, important new features in  $\tau^{-1}(\omega)$  are observed for OP Bi2212 as highlighted in Fig. 2(c). The high-frequency part of  $\tau^{-1}(\omega)$  is fitted with a straight line and the slopes of these linear fits are almost identical for different temperatures. At 200 K,  $\tau^{-1}(\omega)$  increases linearly with frequency. However, deviations from this linear behavior are observed as a suppression of  $\tau^{-1}(\omega)$  at low frequencies above  $T_c$  at 100 K and an “overshoot” of  $\tau^{-1}(\omega)$  at around 900  $\text{cm}^{-1}$  below  $T_c$  at 6 K. The overshoot of  $\tau^{-1}(\omega)$  in OP Bi2212 is very similar to what has been observed in OP YBCO (Ref. 14) and this overshoot has been argued to be the key evidence for boson-mediated superconductivity.<sup>15</sup> Even though the suppression of  $\tau^{-1}(\omega)$  in the normal state has often been interpreted in terms of a

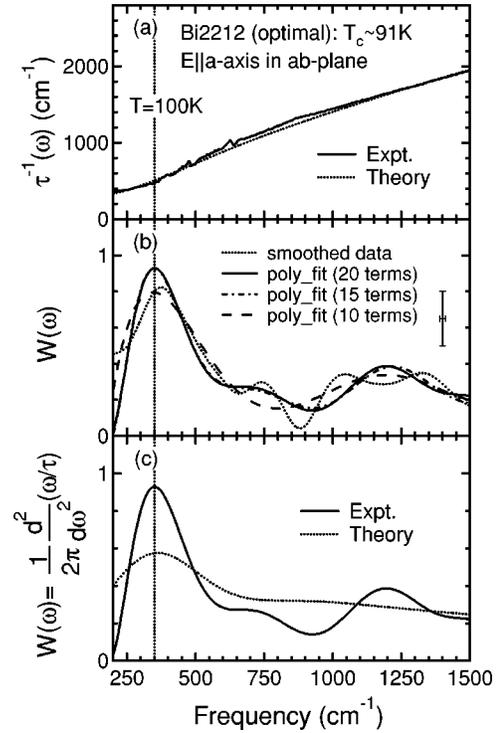


FIG. 3. An unambiguous method of extracting the spectral function  $W(\omega)$ . (a) The experimentally  $\tau^{-1}(\omega)$  at 100 K for OP Bi2212, together with the theoretical calculation, (b) experimentally determined  $W(\omega)$  using different methods (error bar for the derivative analysis is included), and (c) a comparison of experimentally and theoretically determined  $W(\omega)$ .

pseudogap,<sup>13</sup> it is more natural to explain the observed suppression of  $\tau^{-1}(\omega)$  at 100 K here as due to electron-boson coupling. In fact, given that the pseudogap in high- $T_c$  cuprates may have a spin origin, these two interpretations are consistent with each other.

The electron-boson interactions can be studied using  $\tau^{-1}(\omega)$  in more detail. Carbotte *et al.*<sup>6</sup> and Abanov *et al.*<sup>7</sup> analyzed  $\tau^{-1}(\omega)$  in high- $T_c$  cuprates by defining a spectral function  $W(\omega)$  using the Allen formula

$$W(\omega) = \frac{1}{2\pi} \frac{d^2}{d\omega^2} \left[ \frac{\omega}{\tau(\omega)} \right]. \quad (2)$$

It was first pointed out by Allen<sup>3</sup> that  $W(\omega)$  is closely related to the electron-phonon spectral function  $\alpha^2 F(\omega)$  or any other electron-boson spectral function in the normal state for  $T=0$  and in the weak-coupling limit. Shulga<sup>15</sup> rederived the Allen formula in the strong-coupling case and in general for  $T>0$  the electron-boson spectral function is broadened.<sup>5</sup> On these theoretical bases, analyzing  $\tau^{-1}(\omega)$  at 100 K in OP Bi2212 using Eq. (2) in terms of a bosonic spectral function is both mathematically and physically valid.

In Fig. 3 a unique way of extracting the spectral function  $W(\omega)$  from the experimental data is presented. The measured  $\tau^{-1}(\omega)$  at 100 K is plotted for OP Bi2212 in Fig. 3(a), together with the theoretical curve for  $\tau^{-1}(\omega)$  calculated using a model developed by Schachinger and Carbotte.<sup>16</sup> In Fig. 3(b), the spectral function  $W(\omega)$  derived from different

methods using Eq. (2) is plotted. The  $W(\omega)$  determined from the smoothed  $\omega/\tau$  gives a similar spectrum with a maximum at  $350 \text{ cm}^{-1}$  or  $43 \text{ meV}$  determined from the polynomial fits. However, in this study fitting the measured quantity  $\omega/\tau$  with a high-order polynomial is adopted as the unambiguous method of extracting  $W(\omega)$  from the optical data. In Fig. 3(c), the experimentally and theoretically derived  $W(\omega)$  functions are compared and both spectral functions contain a peak at  $43 \text{ meV}$ . It should be emphasized that this  $W(\omega)$  function determined experimentally using Eq. (2) is an approximate one but it qualitatively captures the key features of the true electron-boson spectral function. The main experimental finding is that the suppression of  $\tau^{-1}(\omega)$  at low frequencies at  $100 \text{ K}$  is the result of an electron-boson spectral function peaked around  $43 \text{ meV}$ .

To demonstrate that this  $43 \text{ meV}$  boson in OP Bi2212 is relevant to superconductivity, one has to invert the optical data below  $T_c$ . However, this is a complicated procedure for  $d$ -wave high- $T_c$  cuprates. A formal inversion of the optical data below  $T_c$  is beyond the scope of this experimental work. Fortunately, a simplified visual accessibility procedure is devised by Shulga<sup>15</sup> for “by eye” analysis of the raw optical data below  $T_c$  in terms of electron-boson coupling. In particular, he showed that the ratio of the  $\tau_s^{-1}(\omega)/\tau_n^{-1}(\omega)$  will exhibit a maximum and the ratio of  $R_s(\omega)/R_n(\omega)$  will have a minimum near the frequency of  $2\Delta + \Omega_{max}$ , where  $\Delta$  is the superconducting gap maximum and  $\Omega_{max}$  is the maximum of the electron-boson spectral function.<sup>15</sup> This is because the coherent scattering rate below  $T_c$  grows faster than in the normal state, thereby producing an “overshoot” in  $\tau_s^{-1}(\omega)$  which peaks at around  $2\Delta + \Omega_{max}$ . In Fig. 4(a), such ratios of the reflectance and the scattering rate are given for OP Bi2212. Interestingly, the phonon at  $44 \text{ meV}$  which is absent above  $T_c$  with  $E\parallel a$  axis becomes infrared active below  $T_c$  as shown clearly in the scattering rate ratio in Fig. 4(a) and it has much larger linewidth compared to the other two phonons at  $6 \text{ K}$ . It is evident that a maximum in the ratio of  $\tau_{6K}^{-1}(\omega)/\tau_{100K}^{-1}(\omega)$  and a minimum in the ratio of  $R_{6K}(\omega)/R_{100K}(\omega)$  at around  $900 \text{ cm}^{-1}$  or  $110 \text{ meV}$  can be identified. Taking this value as  $2\Delta + \Omega_{max}$  and using the measured value of  $\Delta = 34 \text{ meV}$  (Ref. 17) for OP Bi2212, a value of  $42 \text{ meV}$  is determined for  $\Omega_{max}$ . This is in excellent agreement with the maximum of the bosonic spectral function at  $43 \text{ meV}$  derived at  $100 \text{ K}$ , indicating that this bosonic spectral function is directly involved in the pair formation in OP Bi2212.

Obviously, the origin of the  $43 \text{ meV}$  boson is an important question. Carbotte *et al.*<sup>6</sup> and Abanov *et al.*<sup>7</sup> argued that the  $43 \text{ meV}$  peak in  $W(\omega)$  corresponds to the spin resonance peak. Furthermore, the spectral function  $W(\omega)$  below  $T_c$  does contain useful information. Carbotte *et al.*<sup>6</sup> showed that for high- $T_c$  cuprates, the strong peak in  $W(\omega)$  below  $T_c$  is correlated with the electron-spin excitation spectral density,  $I^2\chi''(\omega)$ , but shifted to  $\Delta + \Delta_s$ , where  $\Delta_s$  is the maximum of the spin resonance peak. Also, Abanov *et al.*<sup>7</sup> showed that features in  $W(\omega)$  below  $T_c$  are related to the singularities in optical conductivity and they argued that the negative mini-

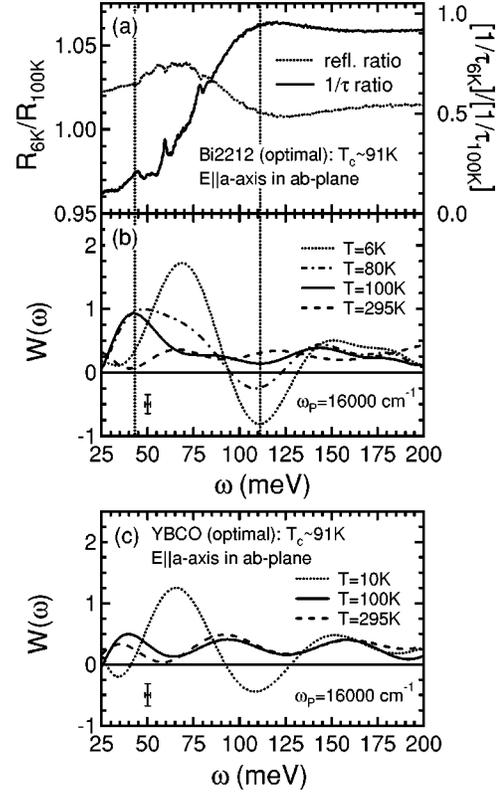


FIG. 4. The temperature dependence of the spectral function  $W(\omega)$  of an OP Bi2212 single crystal and a detwinned OP YBCO single crystal with  $E\parallel a$  in the  $ab$  plane (20-term polynomial fits are used). (a) The reflectance ratio and the scattering rate ratio below and above  $T_c$ , (b)  $W(\omega)$  of an OP Bi2212 single crystal at four different temperatures (error bar for the derivative analysis is included), and (c)  $W(\omega)$  of an OP YBCO single crystal at three different temperatures (error bar for the derivative analysis is included).

mum in  $W(\omega)$  at  $2\Delta + \Delta_s$  is the signature of spin-mediated superconductivity. They also identified two weaker features at  $4\Delta$  and  $2\Delta + 2\Delta_s$ .

The temperature-dependent  $W(\omega)$  is shown in Fig. 4(b) for an OP Bi2212 single crystal. There is a large maximum in  $W(\omega)$  at around  $70 \text{ meV}$ , a deep negative minimum around  $110 \text{ meV}$ , and a weak maximum around  $150 \text{ meV}$  at  $6 \text{ K}$ . According to Carbotte *et al.*<sup>6</sup> and Abanov *et al.*<sup>7</sup> the large maximum corresponds to  $\Delta + \Delta_s$ , the deep minimum should be at  $2\Delta + \Delta_s$ , and the weak maximum at around  $150 \text{ meV}$  is related to  $2\Delta + 2\Delta_s$ . From these observations, one can uniquely determine the values of  $\Delta = 35 \pm 3 \text{ meV}$  and  $\Delta_s = 40 \pm 3 \text{ meV}$ . These optically obtained values agree very well with the directly measured values of  $\Delta = 34 \text{ meV}$  (Ref. 17) and  $\Delta_s = 43 \text{ meV}$  (Ref. 18) for OP Bi2212. Just above  $T_c$  at  $T = 100 \text{ K}$ ,  $W(\omega)$  has a peak at  $43 \text{ meV}$ . However,  $W(\omega)$  becomes featureless at  $T = 295 \text{ K}$ . The  $W(\omega)$  functions for a detwinned OP YBCO single crystal are shown in Fig. 4(c) for comparison. One can again determine the values of  $\Delta = 30 \pm 4 \text{ meV}$  and  $\Delta_s = 40 \pm 4 \text{ meV}$  from the optical data at  $6 \text{ K}$ .<sup>19</sup> These optically obtained values also agree very well with the directly measured values of  $\Delta = 27 \text{ meV}$  (Ref. 20) and  $\Delta_s = 41 \text{ meV}$  (Ref. 21) for OP YBCO. The existence of a

maximum at  $\Delta + \Delta_s$  and a minimum at  $2\Delta + \Delta_s$  in  $W(\omega)$  below  $T_c$  is unique for spin-mediated superconductivity and these characteristic features are absent for a nonsuperconducting ( $\text{Bi}_{0.5}\text{Pb}_{0.5}$ )<sub>2</sub> $\text{Ba}_3\text{Co}_2\text{O}_\delta$  metallic sample. In all, the experimental data are consistent with the picture of spin-mediated superconductivity and the features in  $W(\omega)$  below  $T_c$  can lead to the determination of  $\Delta$  and  $\Delta_s$  optically.<sup>22</sup>

The origin of the 43 meV boson in OP Bi2212 deserves some further discussion. The obvious candidate is the spin resonance peak at 43 meV since it has a similar temperature dependence as well as having the same energy. This is also the conclusion of recent photoemission<sup>23</sup> and tunneling<sup>24</sup> work on Bi2212. The observation of the 43 meV peak at 100 K would imply the existence of a pseudogap above  $T_c$  in OP Bi2212. It should be pointed out that the whole spin excitation spectrum is likely to be involved in the pairing. The spin resonance peak serves as a distinct spectroscopic signature for many types of experiments. Because the spectral function  $W(\omega)$  is featureless at 295 K, this is inconsistent with the suggestion of electron coupling to a zone boundary phonon at 60–80 meV.<sup>8</sup> However, the spectral function analysis alone does not exclude other coupling mechanisms. In particular, the possibility that the electron-boson spectral function is in part the result of electron-phonon coupling cannot be ruled out and our suggestion that the 44 meV phonon is in

fact a magnetic polaron below  $T_c$  due to the resonant interaction with the spin resonance peak should be considered. The appearance of the 44 meV phonon in the  $E||a$  axis spectra below  $T_c$  (presumably becoming infrared active due to interaction with the spin resonance peak) and its large width at 6 K add support to the resonant interaction picture. In the final analysis both spins and phonons can be important for superconductivity in high- $T_c$  cuprates, but the most relevant spectroscopic feature, deduced from these optical measurements for OP Bi2212, is around 40 meV.

In conclusion, we have carried out a detailed analysis of the optical data for OP Bi2212 and OP YBCO single crystals. Our data are consistent with the picture of electron-boson-mediated superconductivity in high- $T_c$  cuprates instead of theories that are based on kinetic energy mechanisms. A detailed theoretical analysis of our high-quality optical data, particularly for OP Bi2212, will lead to a better understanding of the charge dynamics in these systems that is most essential to the superconducting mechanism.

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<sup>1</sup>J.P. Carbotte, *Phys. Canada* **56**, 257 (2000).

<sup>2</sup>W.L. McMillian and J.M. Rowell, *Phys. Rev. Lett.* **14**, 108 (1965).

<sup>3</sup>P.B. Allen, *Phys. Rev. B* **3**, 305 (1971).

<sup>4</sup>B. Farnworth and T. Timusk, *Phys. Rev. B* **10**, 5119 (1976).

<sup>5</sup>F. Marsiglio, T. Startseva, and J.P. Carbotte, *Phys. Lett. A* **245**, 172 (1998).

<sup>6</sup>J.P. Carbotte, E. Schachinger, and D.N. Basov, *Nature (London)* **401**, 354 (1999).

<sup>7</sup>A. Abanov, A.V. Chubukov, and J. Schmalian, *Phys. Rev. B* **63**, 180510(R) (2001).

<sup>8</sup>A. Lanzara *et al.*, *Nature (London)* **412**, 510 (2001).

<sup>9</sup>J.J. Tu *et al.*, *Phys. Rev. Lett.* **87**, 277001 (2001).

<sup>10</sup>M.A. Quijada *et al.*, *Physica C* **235-240**, 1123 (1994); A.V. Puchkov *et al.*, *Phys. Rev. Lett.* **77**, 3212 (1996); M.A. Quijada *et al.*, *Phys. Rev. B* **60**, 14 917 (1999); N.L. Wang *et al.*, *Phys. Rev. B* **59**, 576 (1999).

<sup>11</sup>C.C. Homes, M. Reedyk, D. Crandles, and T. Timusk, *Appl. Opt.* **32**, 2976 (1993).

<sup>12</sup>S.L. Cooper *et al.*, *Phys. Rev. B* **38**, 11 934 (1988).

<sup>13</sup>A.V. Puchkov, D.N. Basov, and T. Timusk, *J. Phys. C* **8**, 10 049 (1996).

<sup>14</sup>D.N. Basov *et al.*, *Phys. Rev. Lett.* **77**, 4090 (1996).

<sup>15</sup>S.V. Shulga, in *Material Science, Fundamental Properties and Future Electronic Applications of High-Tc Superconductors*, edited by S.-L. Drechsler and T. Mishonov (Kluwer Academic Publishers, Dordrecht, 2001), pp. 323–360.

<sup>16</sup>E. Schachinger and J.P. Carbotte, *Phys. Rev. B* **62**, 9054 (2000); **64**, 094501 (2001).

<sup>17</sup>M. Rübhausen *et al.*, *Phys. Rev. B* **58**, 3462 (1998).

<sup>18</sup>H.F. Fong *et al.*, *Nature (London)* **398**, 588 (1999).

<sup>19</sup>C.C. Homes *et al.*, *Phys. Rev. B* **60**, 9782 (1999).

<sup>20</sup>M.F. Limonov *et al.*, *Phys. Rev. B* **61**, 12 412 (2000).

<sup>21</sup>P. Bourges *et al.*, in *High Temperature Superconductors*, edited by S. E. Barnes (American Institute of Physics, Amsterdam, 1999), p. 202.

<sup>22</sup>E. Schachinger, J.P. Carbotte, and D.N. Basov, *Europhys. Lett.* **54**, 380 (2001).

<sup>23</sup>P.D. Johnson *et al.*, *Phys. Rev. Lett.* **87**, 177007 (2001).

<sup>24</sup>J.F. Zasadzinski *et al.*, *Phys. Rev. Lett.* **87**, 067005 (2001).